

**Review from Last Lecture:**

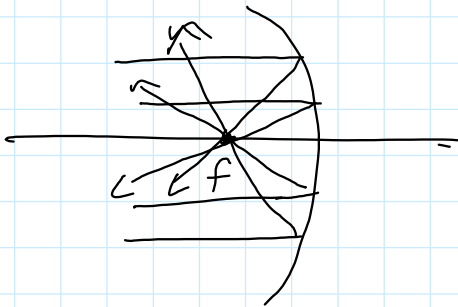
- 1) Understand image formation by spherical mirrors, including the mirror equation, focal length, and magnification

**Goals for this Lecture:**

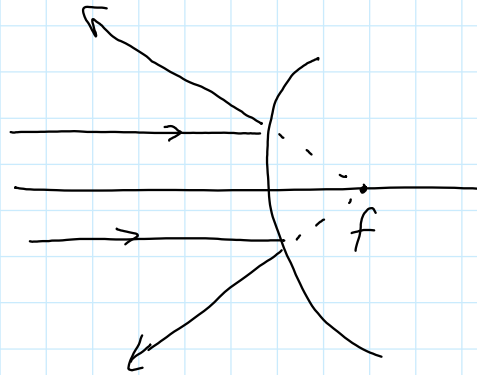
- 2) Understand image formation from refraction, including the equation for refracting surfaces, magnification, and the sign conventions for these equations
- 3) Understand image formation by thin lenses, including the lens maker's equation and the thin lens equation, focal length, magnification, and the sign conventions for these equations

Spherical mirror

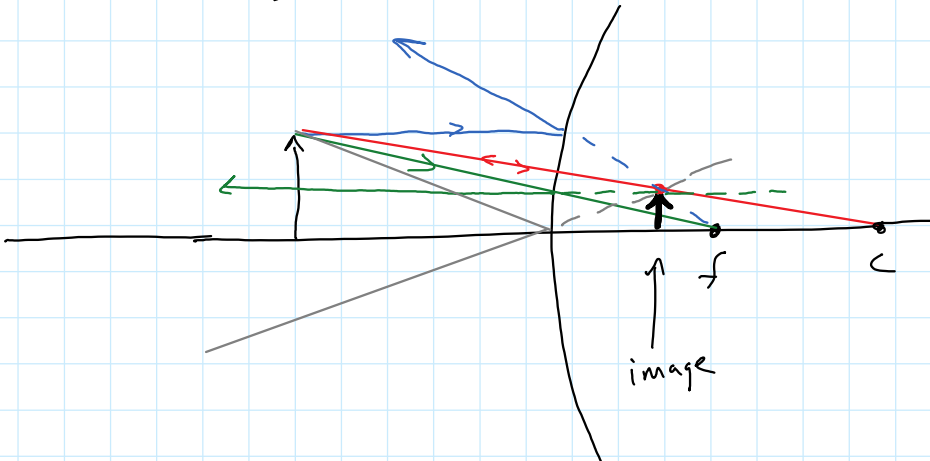
Concave  
or  
converging



Convex  
or  
diverging



Diverging Mirror

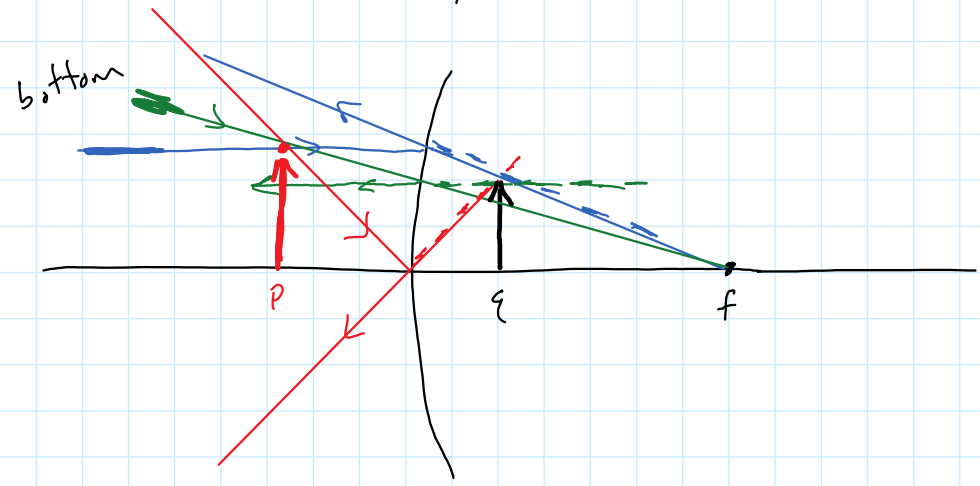
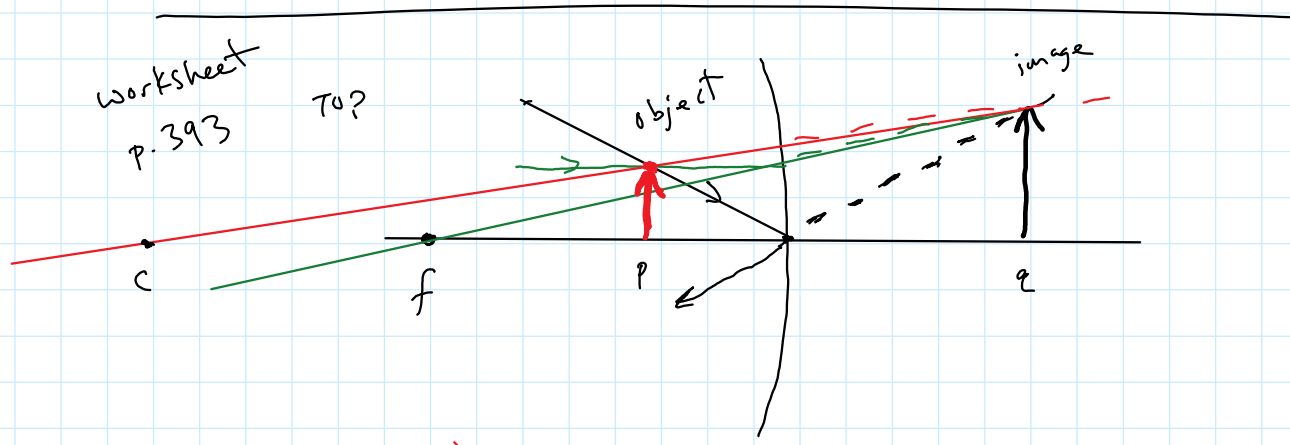


-ksheet

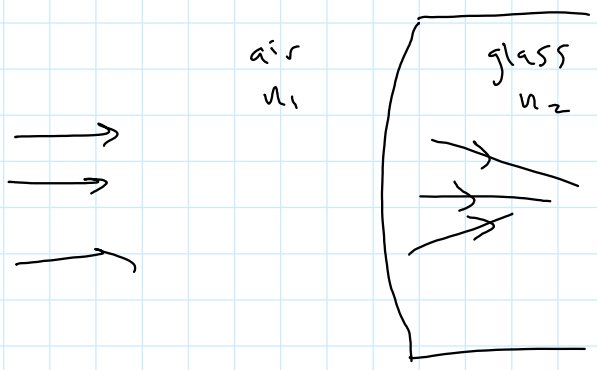
+ 1

image

Worksheet  
p. 393



Images formed by refraction:



Front is where the light originates  
(also defines  $n_1$ )

$$\frac{n_1}{p} + \frac{n_2}{q} = \frac{n_2 - n_1}{R}$$

↖ radius of curvature

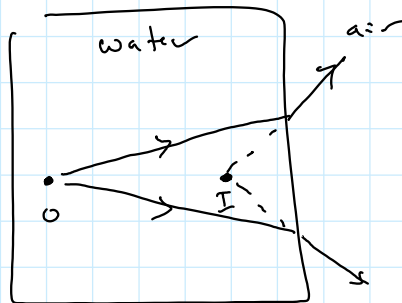
Sign convention:

	+	-
P	on front	on back
q	on back	on front
h'	up right	inverted
R	on Back	on front

} Negative R

Examples

1)



observer

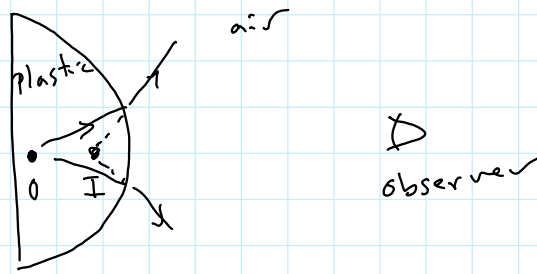
Front side: water  
 $n_1$ :  $n_{\text{water}}$   
 $n_2$ :  $n_{\text{air}}$   
 $R$ :  $\infty$

$$\frac{n_1}{P} + \frac{n_2}{q} = 0$$

$$q = -\frac{n_2}{n_1} P$$

$\uparrow$                        $\uparrow$                        $\uparrow$   
 -                              +                              +

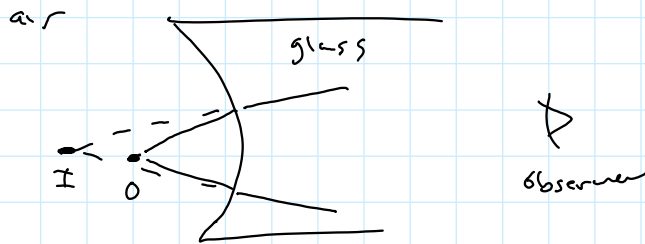
2)



Front : Plastic  
 $n_1$  :  $n_{\text{plastic}}$   
 $n_2$  :  $n_{\text{air}}$

	+	-
P	✓	
q		✓
R		✓

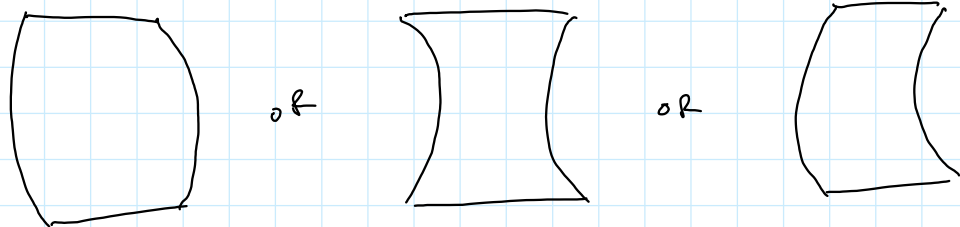
3)



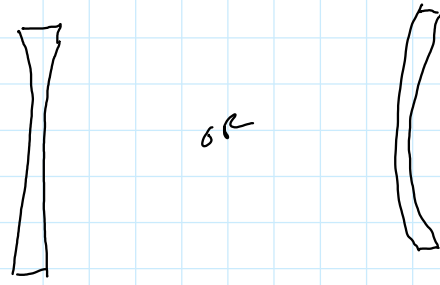
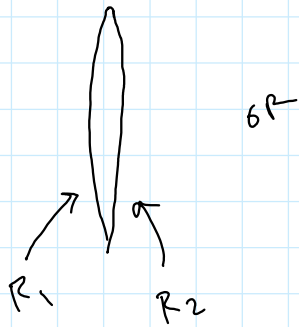
Front : air  
 $n_1$  :  $n_{\text{air}}$   
 $n_2$  :  $n_{\text{glass}}$

	+	-
P	✓	
q		✓
R		✓

Lens has 2 refracting surfaces typically:



if lenses are thin:



Lens maker's Equation

$$\frac{1}{f} = (n-1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$

Thin lens equation

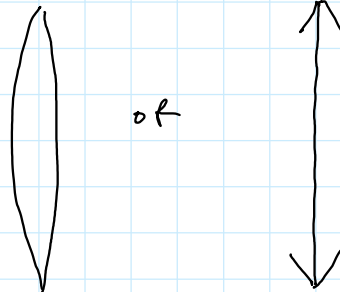
$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$$

Sign convention:

	+	-
$p$	on front	on back
$q$	on back	on front
$h'$	upright	inverted
$f$	converging lens	diverging lens

front is where the light originates

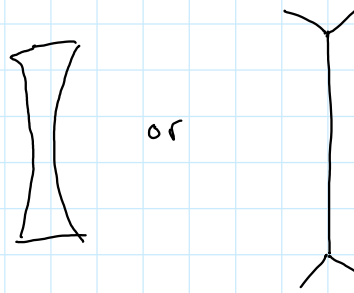
converging lens:



diverging lens:

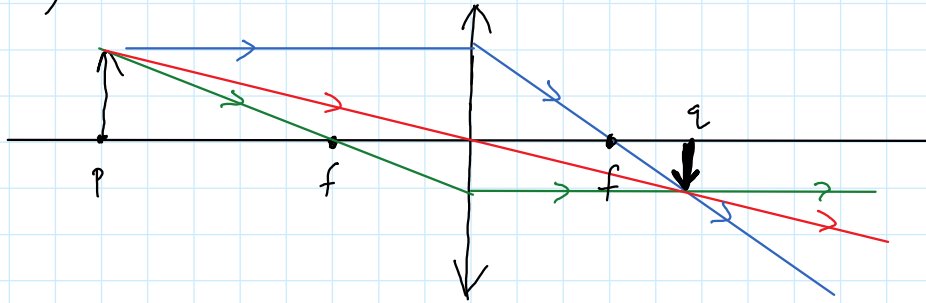


Diverging lens:



## Ray Diagrams

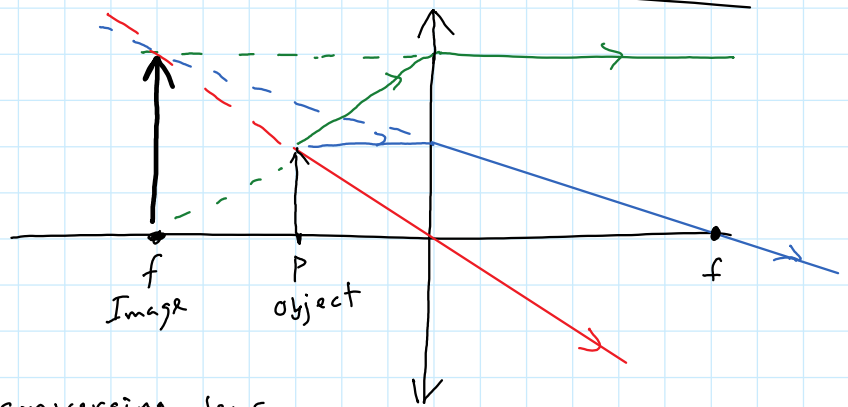
Converging lens:



- 1) In parallel  $\rightarrow$  out through  $f$  on other side
- 2) In through  $f$   $\rightarrow$  out parallel
- 3) In through center of lens  $\rightarrow$  continues in a straight line

Example:

$$\begin{aligned} p &= 30 \text{ cm} \\ f &= 60 \text{ cm} \\ h &= 2 \text{ cm} \end{aligned}$$



$f$  is positive  $\rightarrow$  converging lens

using equations:

$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$$

$$\frac{1}{\dots} + \frac{1}{\dots} = \frac{1}{\dots}$$

$$+30 \quad q \quad +60$$

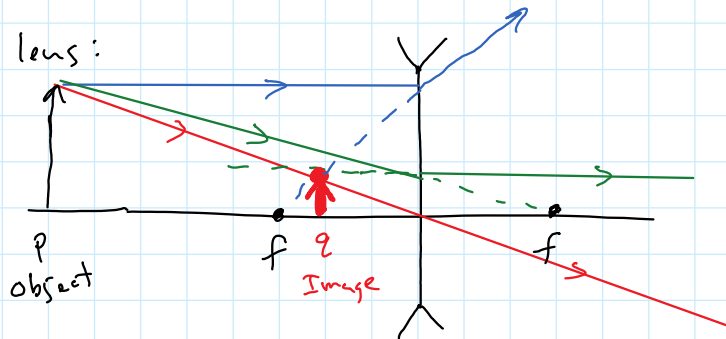
$$q = -60 \text{ cm}$$

$$M = -\frac{q}{p} = -\frac{-60}{30} = +2$$

↑ upright  
twice as big as object

Virtual image

Diverging lens:



1) In parallel → out from f on left

2) In toward f on Right → out parallel

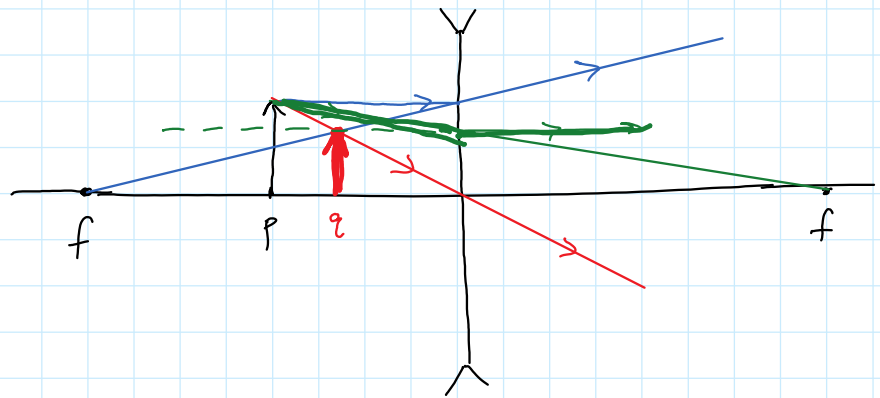
3) In through center of lens → continues in straight line

Example:

$$f = -80 \text{ cm}$$

$$p = 40 \text{ cm}$$

$$h = 2 \text{ cm}$$



$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$$

$$\frac{1}{40} + \frac{1}{q} = \frac{1}{-80}$$

$$q = -26.7 \text{ cm}$$

$$M = -\frac{q}{p} = -\frac{-26.7}{40} = +0.667$$

↑  
upright

Virtual image

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Worksheet  
p. 388

Top:  $n_A > n_B$

Bottom:  $n_B > n_A$

$$V_A > V_B$$

$$n_w \sin \theta_w = n_{oil} \sin \theta_o$$

$$\sin \theta_w = \frac{n_{oil}}{n_w}$$

if  $\theta_w = 50^\circ$  for both cases

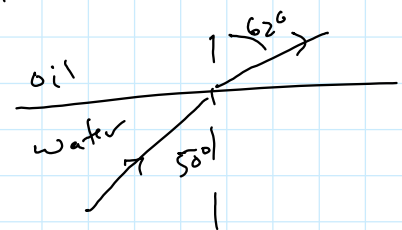
$$n_{water} = 1.5$$

$n_{oil} = 1.3$  gets total internal reflection

if  $n_{oil} = 1.3$

$$1.5 \sin 50 = 1.3 \sin \theta_{oil}$$

$$\theta_{oil} = 62^\circ$$



p. 396

virtual images: A, B, E, F

inverted images: C, D

reduced size images: B, C, D, E, F

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Book Problem  
p. 40

Object located 20 cm to left diverging lens

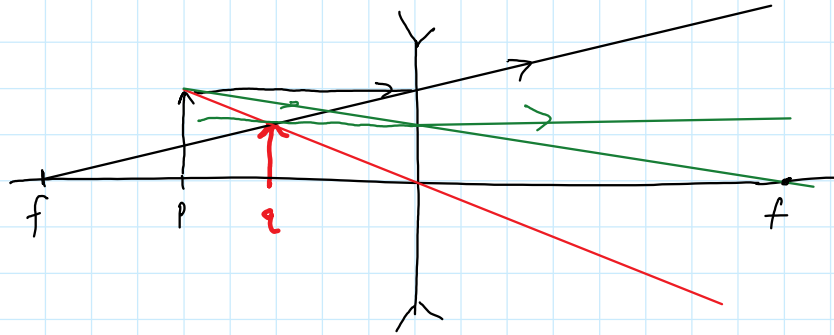


Book Problem  
36-40

Object located 20 cm to left diverging lens  
( $f = -32$  cm)

a) use a ray diagram to solve

b) use equations to solve



$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$$

$$\frac{1}{20} + \frac{1}{q} = \frac{1}{-32}$$

$$q = -12.3 \text{ cm}$$

$$M = -\frac{q}{p} = -\frac{-12.3}{20} = +0.615$$

upright

virtual image