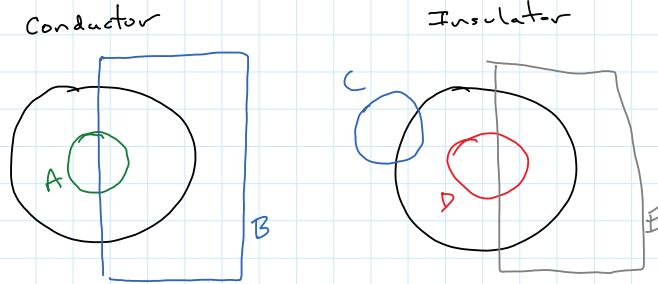


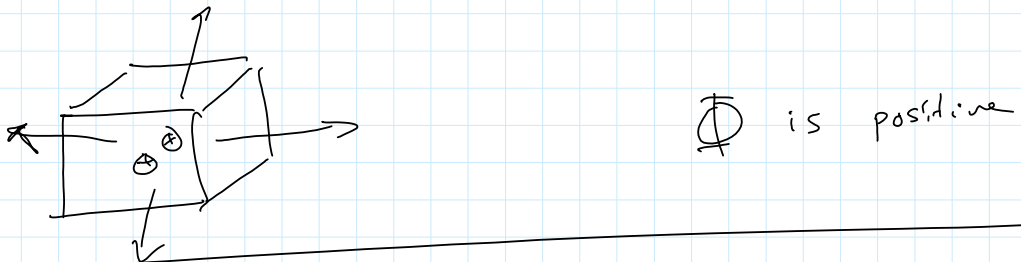
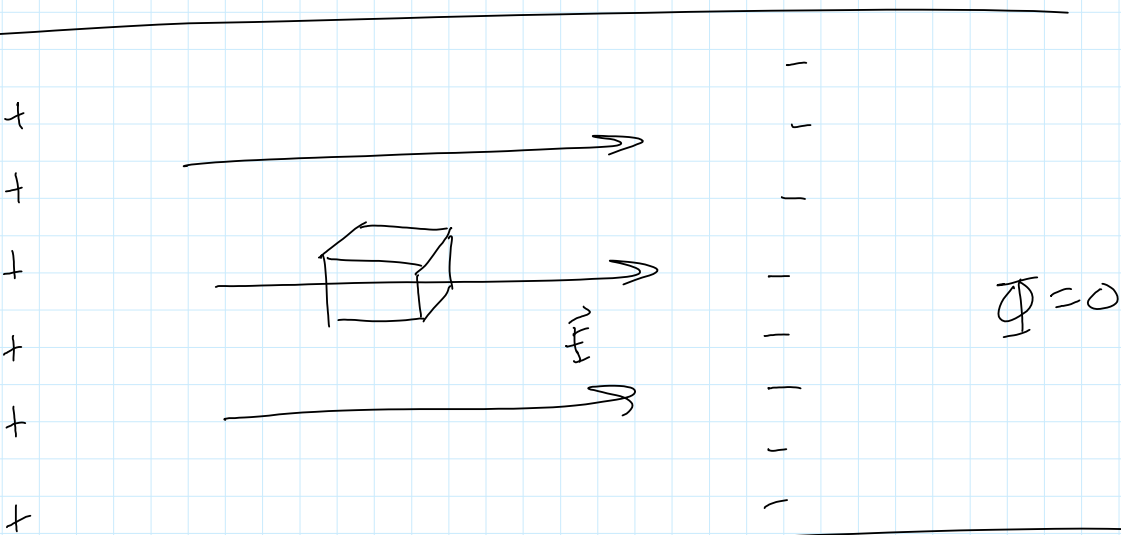
Goals for the Lecture:

- 1) Understand when Gauss's Law is useful in solving problems and be able to use it to solve problems
- 2) Understand properties of conductors in electrostatic equilibrium, including shielding of electric fields

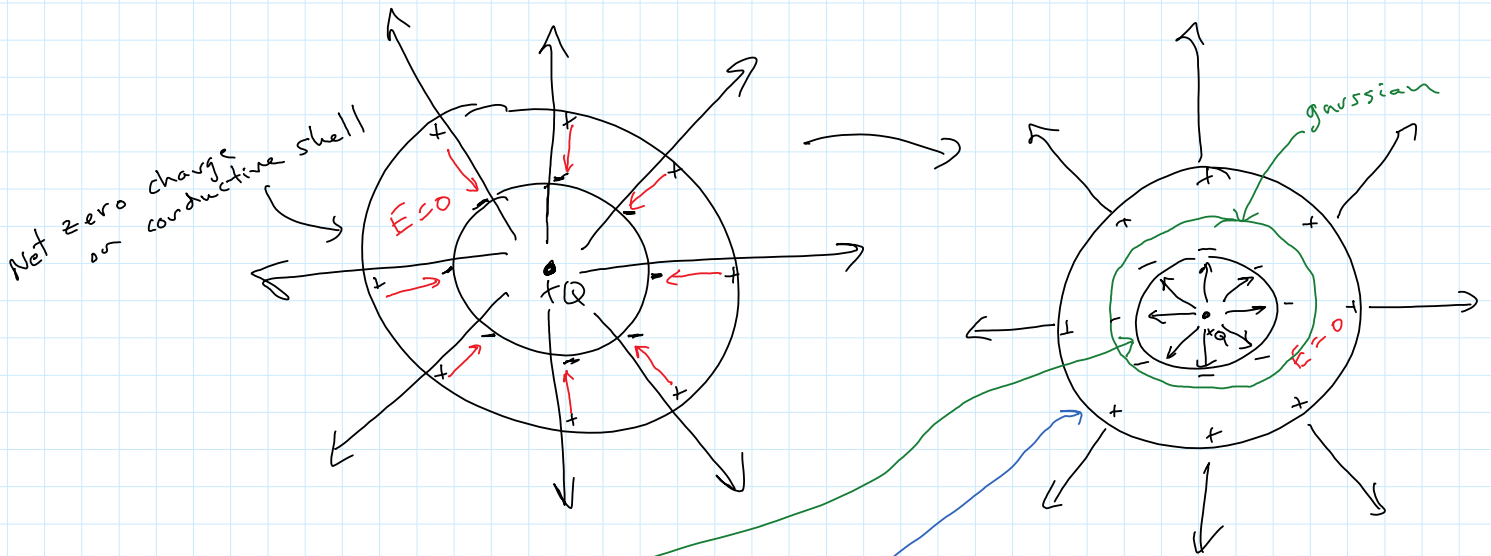
Worksheet
P. 37



$$B = E > D > C > A = 0$$



Conductive shell (Find charge on inner and outer surfaces)



find q_{inner} and q_{outer} :

↑
on inner surface of conductor

↓ inside gaussian surface

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{enclosed}}{\epsilon_0} \text{ for the gaussian surface}$$

$$0 = \frac{q_{enclosed}}{\epsilon_0}$$

$$q_{enclosed} = 0$$

$$\text{So, } q_{inner} = -Q$$

then :

$$q_{inner} + q_{outer} = q_{\text{net charge on conductive shell}}$$

$$q_{inner} + q_{outer} = 0$$

$$q_{outer} = +Q$$

Worksheet
2.40

a) $\Phi_A = \Phi_C$ so, both enclose the same amount of charge

Worksheet
p. 40

a) $\Phi_A = \Phi_C$ so, both enclose the same amount of charge
so, the conductive shell has no net charge

$$\left. \begin{array}{l} q_{\text{inner}} = -Q_0 \\ q_{\text{outer}} = +Q_0 \end{array} \right\} q_{\text{inner}} + q_{\text{outer}} = 0$$

b) $\Phi_C = 3\Phi_A$ so, charge on conductive shell must be $+2Q_0$

$$q_{\text{inner}} = -Q_0 \quad \text{must cancel } +Q_0 \text{ inside cavity}$$

$$q_{\text{inner}} + q_{\text{outer}} = +2Q_0$$

$$q_{\text{outer}} = +3Q_0$$

$$c) \quad \Phi_A = \frac{q_{\text{in}}}{\epsilon_0} = \frac{+Q_0}{\epsilon_0}$$

d) $\Phi_C = 0$ so, Net charge on conductive shell must be $-Q_0$

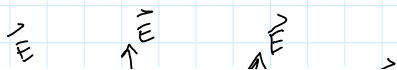
$$q_{\text{inner}} = -Q_0$$

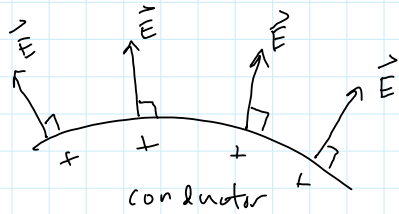
$$q_{\text{inner}} + q_{\text{outer}} = -Q_0$$

$$q_{\text{outer}} = 0$$

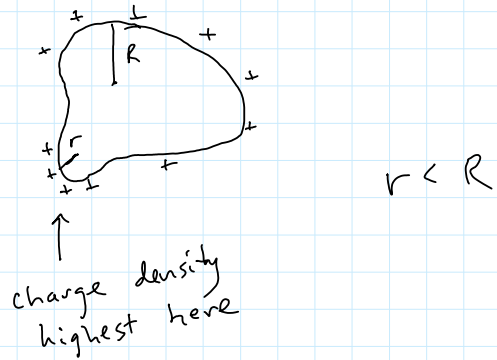
Conductors in electrostatic equilibrium:

- 1) excess charge goes to outer most surface
- 2) $E = 0$ inside conductor
- 3) $E \perp$ to surface (just outside of conductor)



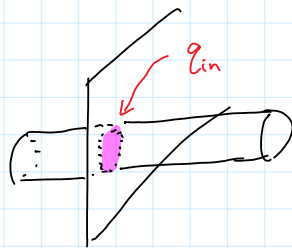


4) surface charge density is greatest where radius of curvature is smallest



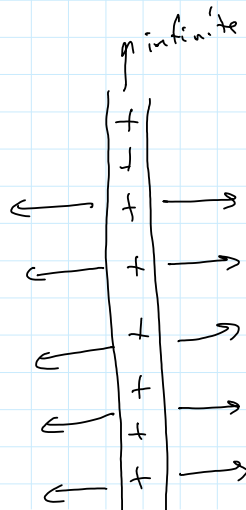
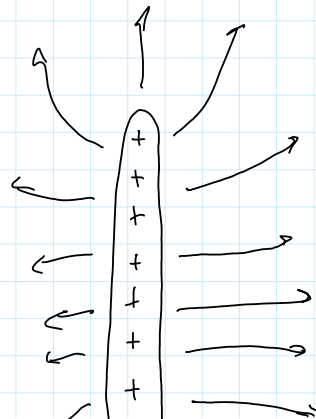
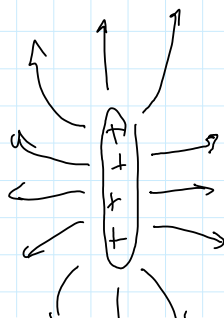
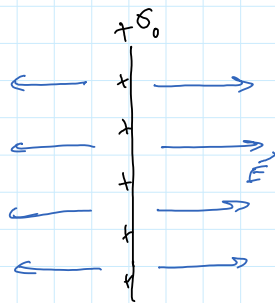
Worksheet
p. 35

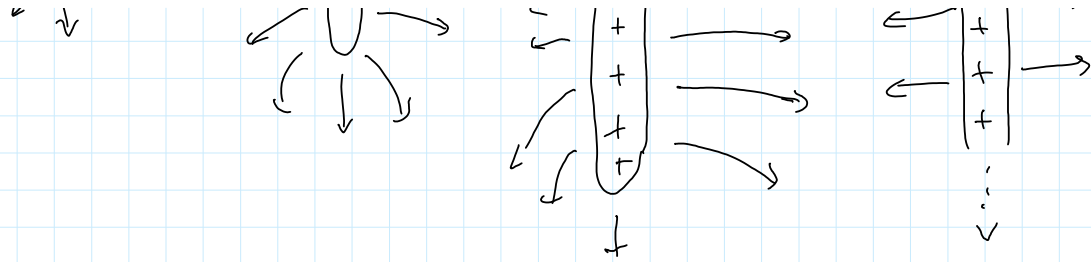
1)



$$q_{in} = A_1 \sigma_0 \quad \text{or} \quad A_2 \sigma_0 \quad \text{since} \quad A_1 = A_2$$

2)



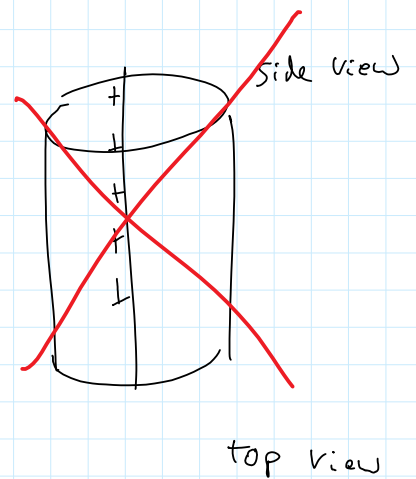
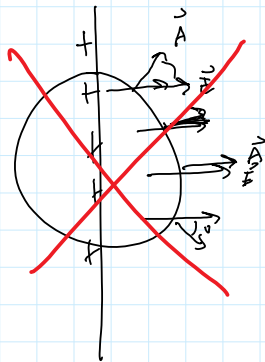
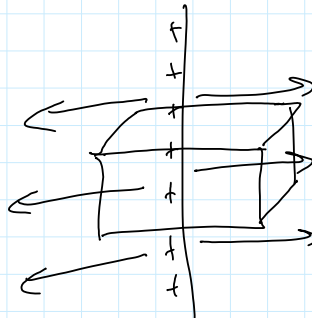


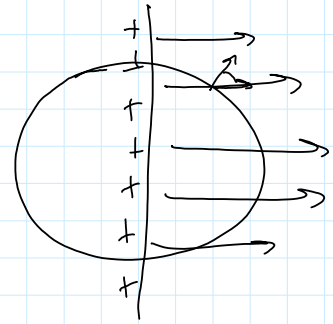
no

3) $E_L = E_R$
 $A_1 = A_2$

4) Φ_1 and Φ_2 are non-zero
 $\Phi_3 = 0$

what other gaussian surface would be a good choice for an infinite sheet of charge?





5) use Gauss's Law to find E:

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

$$\int_{LF} \vec{E} \cdot d\vec{A} + \underbrace{\int_{side} \vec{E} \cdot d\vec{A}}_0 + \int_{RT} \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

$$EA_2 + 0 + EA_1 = \frac{\sigma A_1}{\epsilon_0}$$

$$A_1 = A_2 = A$$

$$2EA = \frac{\sigma A}{\epsilon_0}$$

$$E = \frac{\sigma}{2\epsilon_0}$$

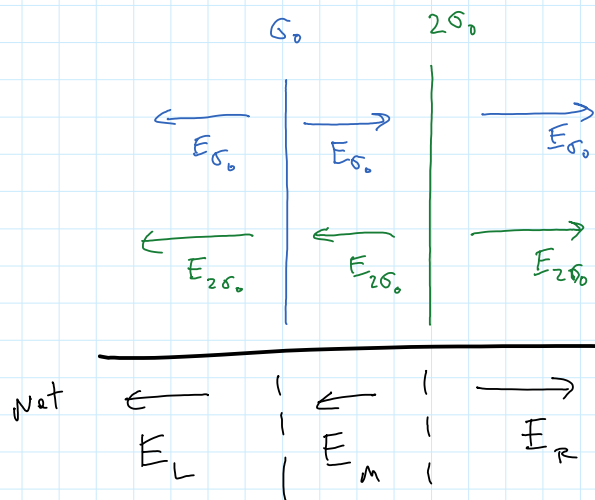
insulating sheet of charge

p. 36

B) 1)

$$q_{in} = \sigma_0 A + 2\sigma_0 A = 3\sigma_0 A$$

2)



$$E_L = E_R = E_{\sigma_0} + E_{2\sigma_0}$$

$$\left(\vec{E}_L = -\vec{E}_R \right)$$

$$E = \frac{\sigma}{2\epsilon_0} \quad \text{in general for an infinite sheet of charge}$$

$$E_{\sigma_0} = \frac{\sigma_0}{2\epsilon_0}$$

$$E_{2\sigma_0} = \frac{2\sigma_0}{2\epsilon_0} = \frac{\sigma_0}{\epsilon_0}$$

$$E_L = E_R = \frac{3\sigma_0}{2\epsilon_0}$$

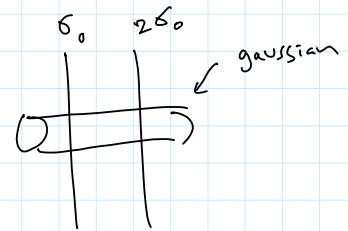
Now, use Gauss's Law: (see if you get the same result)

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

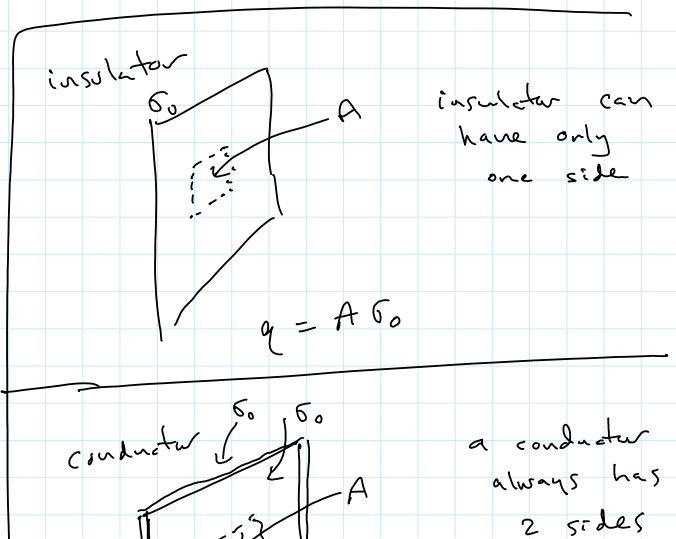
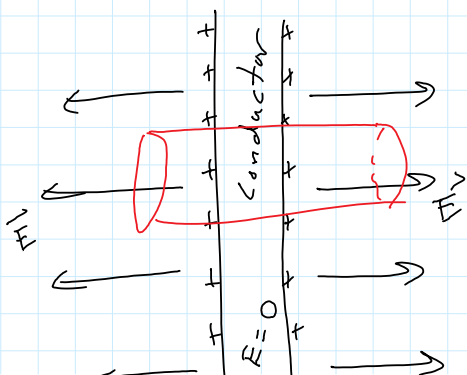
$$\int_L \vec{E} \cdot d\vec{A} + \int_{\text{side}} \vec{E} \cdot d\vec{A} + \int_{R+} \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

$$EA + 0 + EA = \frac{3\sigma_0 A}{\epsilon_0}$$

$$E = \frac{3\sigma_0}{2\epsilon_0}$$



Conductive sheet





$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

$$\int_{LA} \vec{E} \cdot d\vec{A} + \underbrace{\int_{side} \vec{E} \cdot d\vec{A}}_0 + \int_{RA} \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

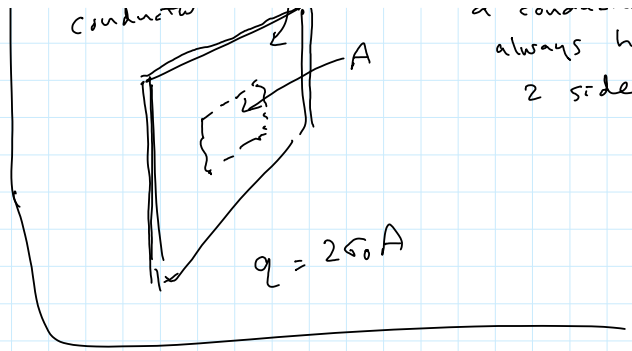
$$EA + 0 + EA = \frac{q_{in}}{\epsilon_0}$$

$$2EA = \frac{q_{in}}{\epsilon_0}$$

$$2EA = \frac{2\sigma A}{\epsilon_0}$$

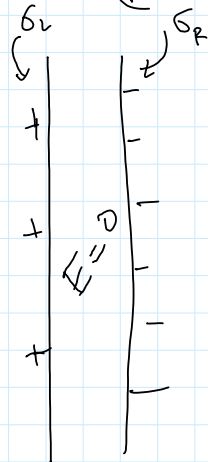
$$E = \frac{\sigma}{\epsilon_0}$$

for a conductive sheet of charge

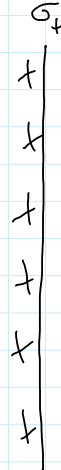


a conductor always has 2 sides

conductive sheet of charge (net negative)



insulating sheet of charge (net positive)



$$\text{Let } \sigma_+ = +10 \frac{\mu\text{C}}{\text{m}^2}$$

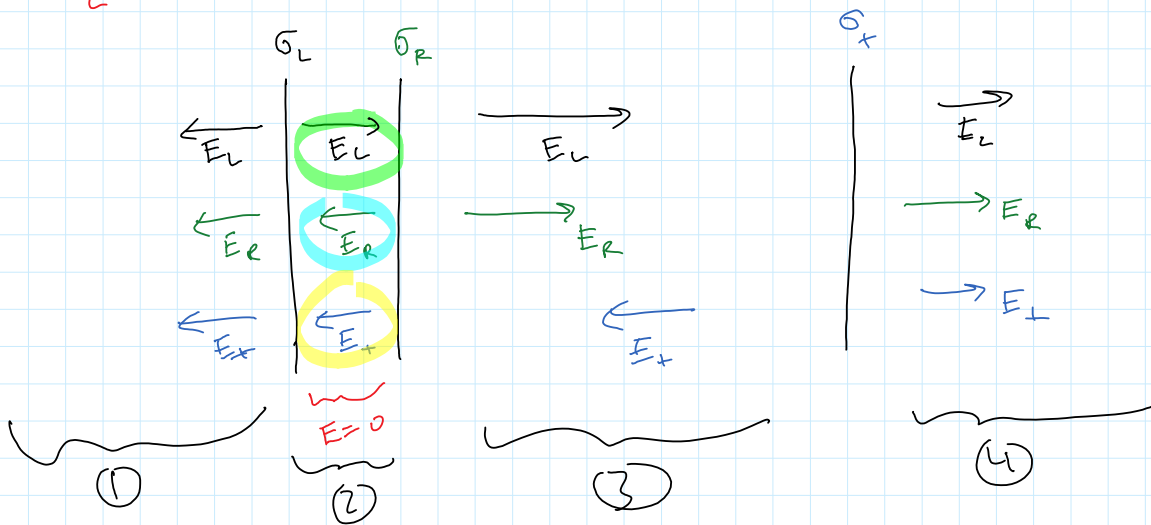
When all alone in space:

$$\sigma_{\text{conductor}} = -6 \frac{\mu\text{C}}{\text{m}^2}$$

Find 1) σ_L and σ_R on conductor after insulator is brought near

2) E everywhere

[Treat them as 3 insulating sheets of charge]



We know:

$$\sigma_L + \sigma_R = 2 \sigma_{\text{conductor}}$$

$$\vec{E}_L + \vec{E}_R + \vec{E}_+ = 0 \quad \text{inside conductor}$$

$$\left(+\right) \frac{\sigma_L}{2\epsilon_0} - \frac{\sigma_R}{2\epsilon_0} - \frac{\sigma_+}{2\epsilon_0} = 0 \quad \rightarrow +$$

$$\sigma_L - \sigma_R - \sigma_+ = 0$$

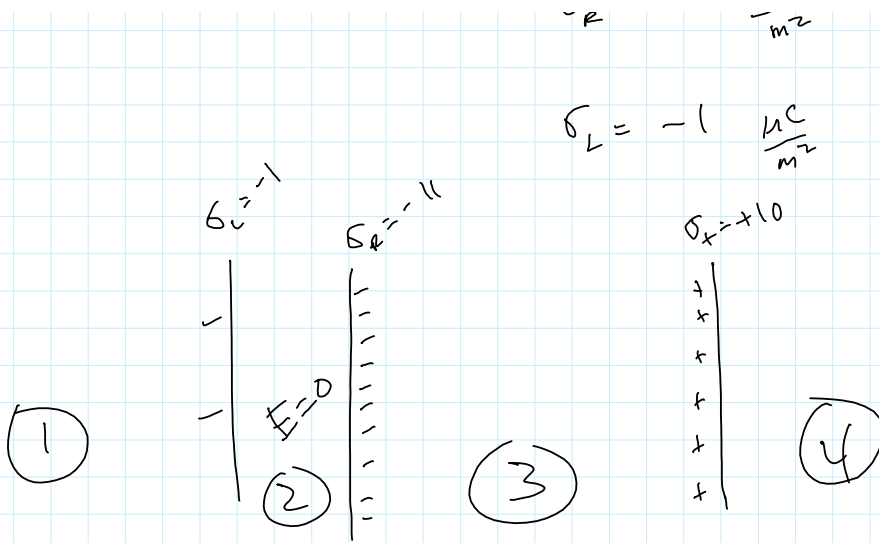
$$\sigma_L - \sigma_R - 10 = 0 \quad (1)$$

$$\sigma_L + \sigma_R = 2(-6) \quad (2)$$

$$10 + \sigma_R + \sigma_R = -12$$

$$2\sigma_R = -22$$

$$\sigma_R = -11 \frac{\mu\text{C}}{\text{m}^2}$$



$$E_1 = -\frac{\sigma_L}{2\epsilon_0} - \frac{\sigma_R}{2\epsilon_0} - \frac{\sigma_+}{2\epsilon_0} = -\frac{(-1)}{2\epsilon_0} - \frac{(-11)}{2\epsilon_0} - \frac{(+10)}{2\epsilon_0} = \frac{2}{2\epsilon_0} = \frac{1}{\epsilon_0}$$

$$= +\frac{1}{\epsilon_0} \rightarrow \left[\begin{array}{l} \text{Positive is} \\ \text{to the right} \end{array} \right]$$

$$E_2 = 0$$

$$E_3 = E_L + E_R - E_+ = \frac{\sigma_L}{2\epsilon_0} + \frac{\sigma_R}{2\epsilon_0} - \frac{\sigma_+}{2\epsilon_0} = \frac{(-1)}{2\epsilon_0} + \frac{(-11)}{2\epsilon_0} - \frac{(+10)}{2\epsilon_0}$$

$$= -\frac{22}{2} \frac{1}{\epsilon_0} = -\frac{11}{\epsilon_0} \quad \left(\begin{array}{l} \text{Negative is} \\ \text{to the left} \end{array} \right)$$

$$E_4 = -\frac{1}{\epsilon_0} \quad \left(\begin{array}{l} \text{Negative is} \\ \text{to the left} \end{array} \right)$$