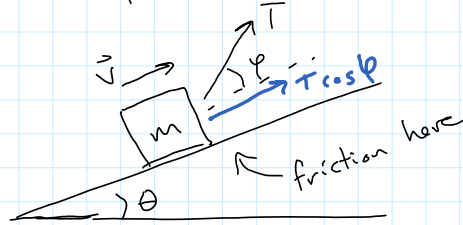


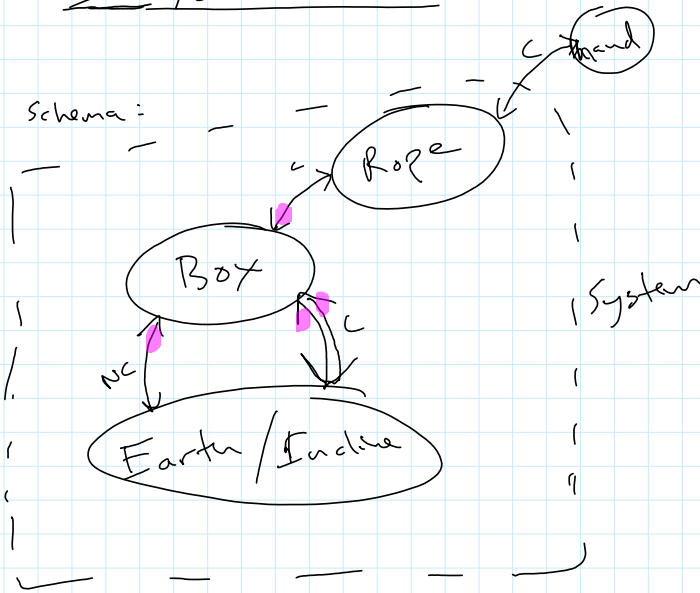
Goals for the Lecture:

- 1) Use Newton's Second Law to solve circular motion problems

Pulling a box up an incline w/ a rope



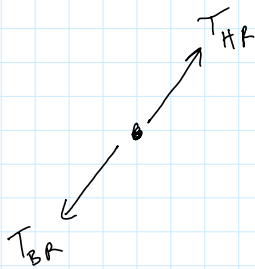
System Schema:



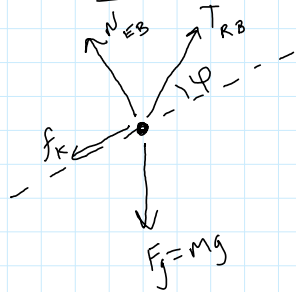
Assume: massless Rope

FBD

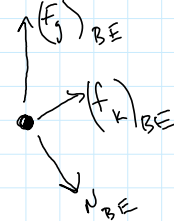
Rope



Box



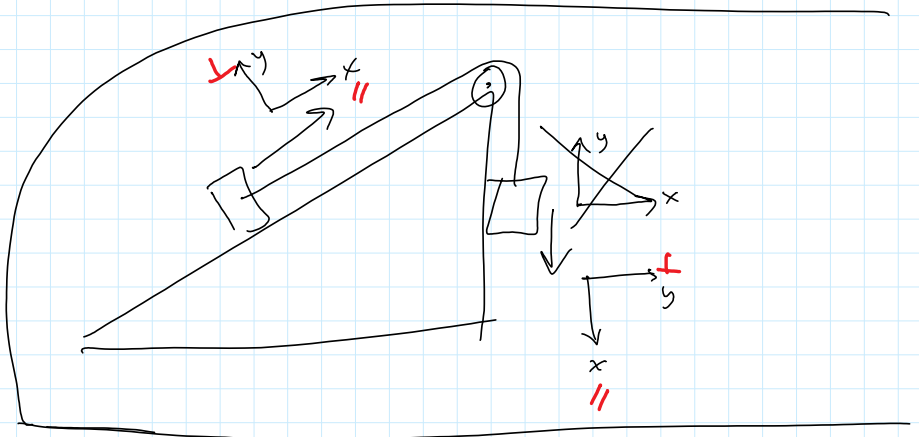
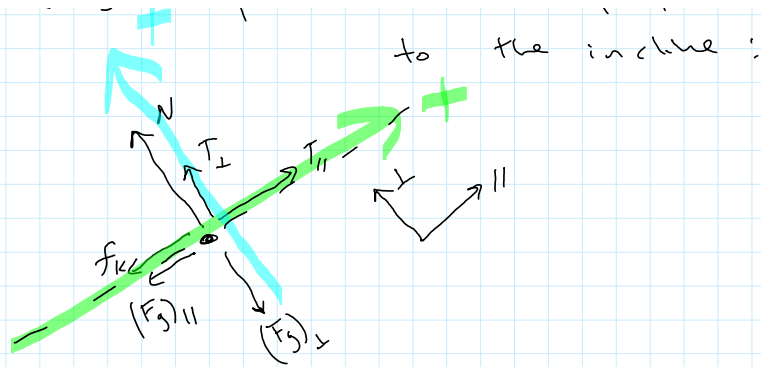
Earth



given:  $\mu_k, m, \theta, \varphi, T$

find:  $a$

use components: parallel and perpendicular to the incline:



$$\sum \vec{F} = m\vec{a}$$

$$\sum F_{||} = m a_{||} \quad \text{up incline}$$

$$T_{||} - f_k - (F_g)_{||} = ma$$

$$\sum F_{\perp} = m a_{\perp}$$

$$N + T_{\perp} - (F_g)_{\perp} = m a_{\perp}$$

$$N + T_{\perp} - (F_g)_{\perp} = 0$$

$$\begin{aligned} F_g &= mg \\ (F_g)_{\perp} &= mg \cos \theta \\ (F_g)_{||} &= mg \sin \theta \\ T_{||} &= T \cos \varphi \\ T_{\perp} &= T \sin \varphi \end{aligned}$$

$$T \cos \varphi - \mu_k N - mg \sin \theta = ma$$

$$N + T \sin \varphi - mg \cos \theta = 0$$

1) solve for N

3) solve for a

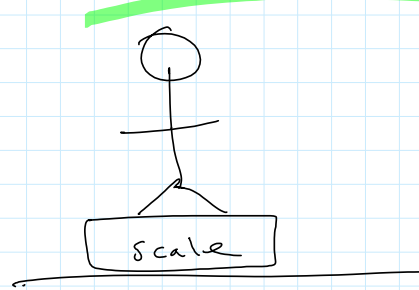
2) solve for N

1) solve for N

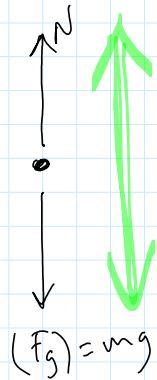
Apparent weight:

mass: how much stuff something is made of  
always the same

weight: gravitational force between object and planet/moon



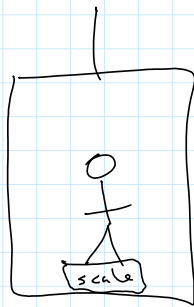
FBD



Person's mass = 50 kg

use  $g = 10 \frac{m}{s^2}$

Elevator



a) Not moving:

$$\Sigma F = 0 \quad \uparrow +$$

$$N = mg = 500 \text{ N}$$

b) starts going down w/  $a = 2 \frac{m}{s^2} \downarrow$

$$\Sigma F = ma \quad \uparrow +$$

$$N - mg = m(-2)$$

$$N = mg - 2m = 400 \text{ N}$$

c)  $v = \text{constant}$  in  $\downarrow$  direction  
( $a = 0$ )

$$N = mg = 500 \text{ N}$$

d) slows down  $a = 2 \frac{m}{s^2} \uparrow$

$$\Sigma F = m a$$

$$N - mg = m(+z)$$

$$N = mg + 2m$$

$$= 600 \text{ N}$$

e) Rope breaks  $\rightarrow$  freefall

$$\Sigma F = m a \uparrow$$

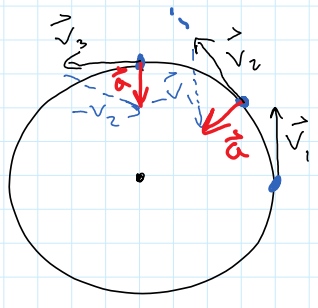
$$N - mg = m(-g)$$

$$N = 0$$

"weightlessness"



Uniform Circular Motion: constant speed



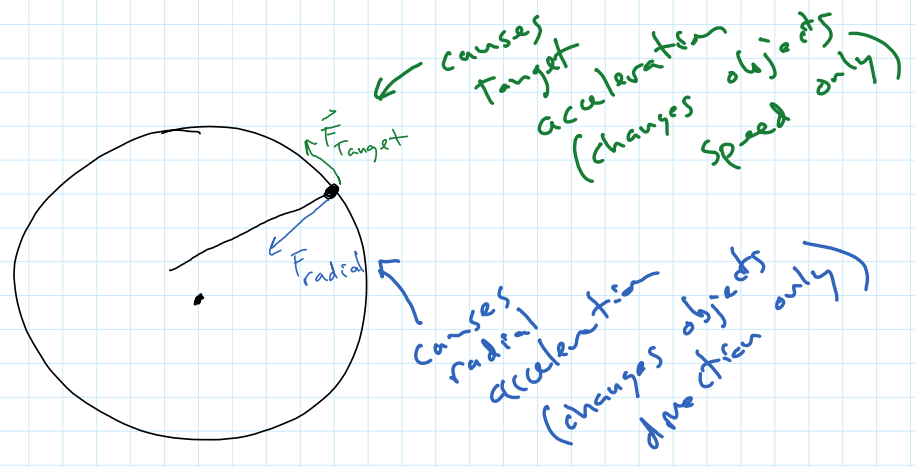
$$|\vec{v}_1| = |\vec{v}_2| = |\vec{v}_3|$$

Find  $\vec{a}$  :

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t} = \frac{\vec{v}_f - \vec{v}_i}{\Delta t}$$

For circular motion

$$a_{\text{radial}} = \frac{v^2}{R} = a_c \quad \text{centripetal acceleration}$$



Centripetal Force

$$F = m a$$

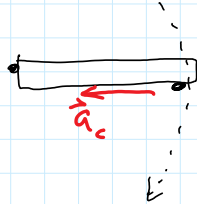
# Centripetal Force

$$F = ma$$

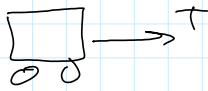
$$F_c = ma_c$$

$$= \frac{mv^2}{R}$$

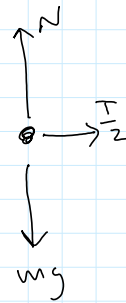
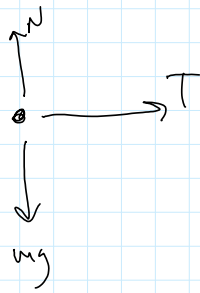
Top view of door



worksheet  
II-20



still speeds up, but at a lower rate



II-21



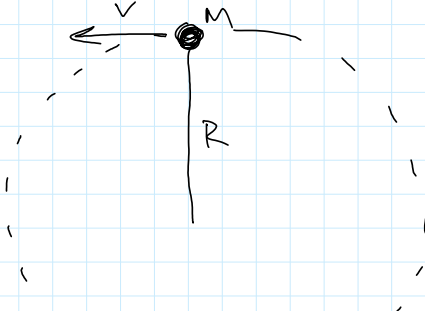
$$\Sigma F = ma \quad \downarrow +$$

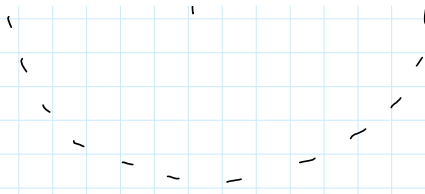
$$mg - T = ma$$

$$T = mg - ma$$

$$T < mg$$

vertical circle: mass on a string  
uniform circular motion: speed is constant =  $v$





given:  $m, R, v$

Find  $T$  in string at Top and bottom of path

bottom



$$\Sigma F = ma \quad \uparrow + \text{(radially inward)}$$

$$T - mg = m\left(\frac{v^2}{R}\right)$$

$$T = mg + \frac{mv^2}{R}$$

Top



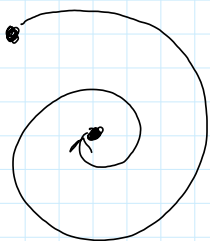
$$\Sigma F = ma$$

$$\Sigma F_{\text{radial}} = ma_c \quad \downarrow + \text{(radially inward)}$$

$$T + mg = \frac{mv^2}{R}$$

$$T = \frac{mv^2}{R} - mg$$

$\Sigma F_{\text{radial}}$



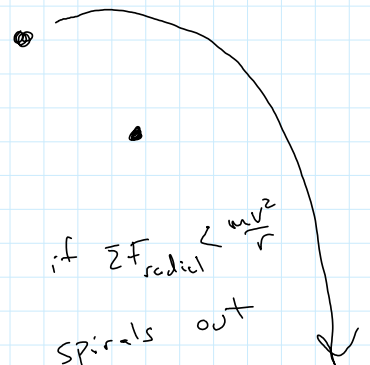
if  $\Sigma F_{\text{radial}} > \frac{mv^2}{R}$

spirals in



if  $\Sigma F_{\text{radial}} = \frac{mv^2}{R}$

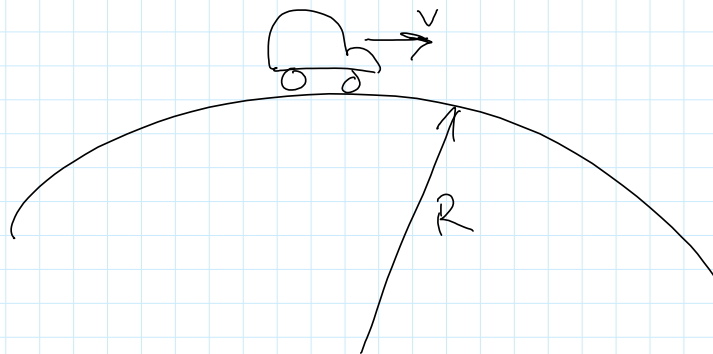
circular motion



if  $\Sigma F_{\text{radial}} < \frac{mv^2}{R}$

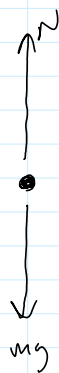
spirals out

Drive over a speed bump:



given :  $m, R$

find :  $V_{max}$  such that car is just in contact with ground



$$\Sigma F_{radial} = m a_c \quad \downarrow +$$

$$mg - N = m \frac{v^2}{R}$$

at  $V_{max}$ ,  $N \rightarrow 0$

$$mg = \frac{m V_{max}^2}{R}$$

$$V_{max} = \sqrt{Rg}$$