

Continuum thermodynamics
ch. 17 and 18

Review session: Thursday Noon - 1:00 pm → 4404

Ideal gas law:

$$P \propto n \quad (\text{number of moles})$$

$$P \propto T \quad \text{temp}$$

$$P \propto \frac{1}{V} \quad \text{volume}$$

$$P = R \frac{nT}{V}$$

$$PV = nRT$$

$$R = 8.31 \frac{\text{J}}{\text{mol K}}$$

$$R = 0.0821 \frac{\text{atm}}{\text{mol K}}$$

OR

$$PV = NkT$$

$k = \text{Boltzman Constant}$

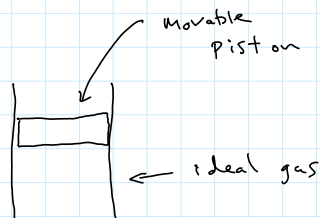
$$= 1.38 \times 10^{-23} \frac{\text{J}}{\text{K}}$$

$N = \# \text{ of molecules}$

Cylinder:

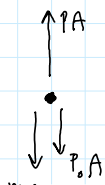
- ideal gas
- room temp
- sealed
- piston free to move without friction

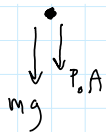
mass: M
area: A



If piston is at rest and atm Pressure = P_0

Draw a FBD for the piston:





Net force on piston is: zero

Which force is larger: $F_{\text{gas inside}}$ or $F_{\text{air outside}}$

$$F_{\text{gas}} > F_{\text{air}}$$

$$\sum \vec{F} = 0$$

$$\vec{F}_{\text{gas}} + \vec{F}_{\text{air}} + \vec{mg} = 0$$

Which is at higher Pressure: gas inside or air outside

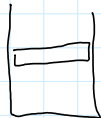
$$P_{\text{gas}} > P_0$$

$$P_{\text{gas}} A = P_0 A + mg$$

$$P_{\text{gas}} = \frac{P_0 A + mg}{A}$$

2nd cylinder contains a different sample

Cylinders are same
both at room temp



original

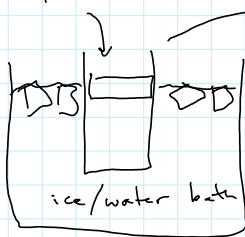


second

Is the Pressure in the 2nd cylinder
greater, less, same as original?

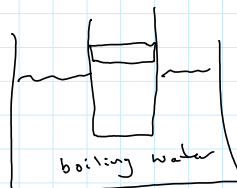
Same

Piston free to move



initial

$$P_i, V_i, T_i$$



final

$$P_f, V_f, T_f$$

Compare T_f to T_i : $T_f > T_i$

f, f, f

1) Compare T_f to T_i : $T_f > T_i$

2) Compare P_f to P_i : $P_f = P_i$ (after some time)
(piston not moving)

3) Compare V_f to V_i : $V_f > V_i$

$$\frac{P}{\text{same}} V = \frac{nRT}{\text{same}}$$

$$V \propto T$$

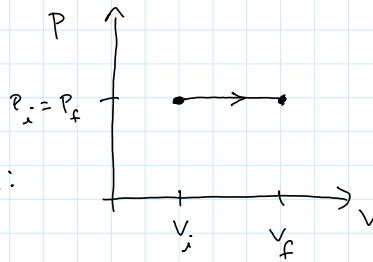
what was constant : P, n

what changed : V, T

PV diagrams

Pressure - Volume

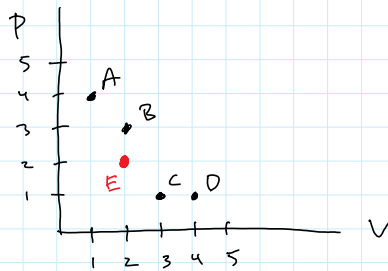
a point represents a state of the system:
 P, V



Draw on the P-V diagram

the process from above (P, n are constant)
(V, T change)

A sample of an ideal gas in a cylinder - Pressure and volume are changed and measured several times



1) Rank the temp in the 4 states :

$$PV = \frac{nRT}{\text{not changing}}$$

$$T \propto PV$$

State	P	V	PV
A	4	1	4
B	3	2	6
C	1	3	3
D	1	4	4

$$T_B > T_A = T_D > T_C$$

2) Is there a state with the volume of B

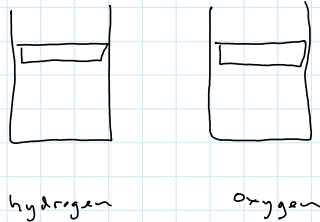
and the temp of A?
 If S_0 , mark it on the PV diagram. (call it E)

Same temp as A: $PV = 4$

Same V as B: $V = 2$

S_0 , $P = 2$

2 identical cylinders
 - same temp
 - pistons at same height



- 1) Compare volumes: same
- 2) Compare temp: same
- 3) Compare Pressure: same
- 4) Compare number of moles: same
 since: $PV = nRT$

H_2 : 2 grams per mol

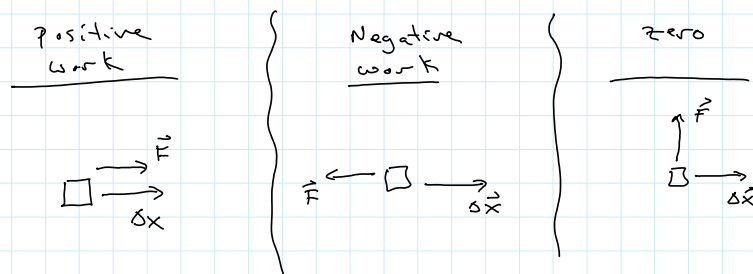
O_2 : 32 grams per mol

$$M_{O_2} > M_{H_2}$$

Work Review:

A) Define work: $W = F \cdot d$ if F is constant and in direction of displacement

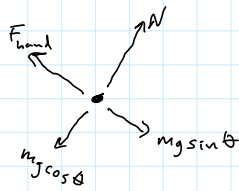
$$W = \vec{F} \cdot \vec{\Delta X} \quad \text{if } F \text{ is constant}$$



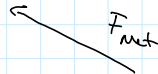
block moves up incline
 with increasing speed



1) FBD for block:



2) direction of net force:



3)

Force	Work done on block
F_{hand}	Positive
F_g	Negative
N	Zero

4) Work done on your hand by the block:

Negative

$$W_{on hand by block} = - W_{on block by hand}$$

$$W_{net} = \Delta K$$

change in kinetic Energy

Ideal gas in cylinder
free to move w/o friction



1) Direction of force piston exerts on gas: ←

Does it depend on the motion of the piston: No

2) How can it move to do

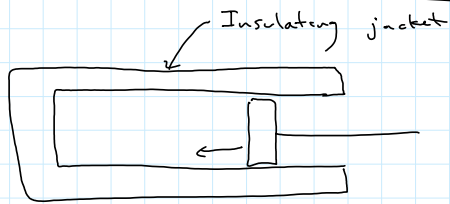
Positive work on gas: to the left

Negative " " " : to the Right

Does it depend on your coordinate system? No

$$W_{AB} = -W_{BA}$$

Cylinder thermally isolated



Press inward on piston
call this step:
Compression 1

In compression 1: Is work done on the gas
by the piston + / - / 0: positive

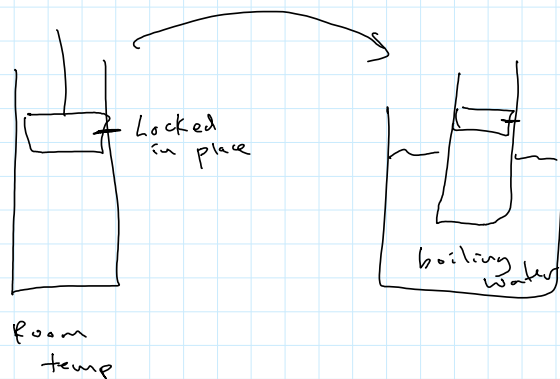
Internal energy: E_{int}

can change E_{int} by +/- heat
or by doing +/- work
on system

For our process above, how does E_{int} change:
increases

Does the temp of the gas change:
increases

Process 2:



In process 2: how do the following change:

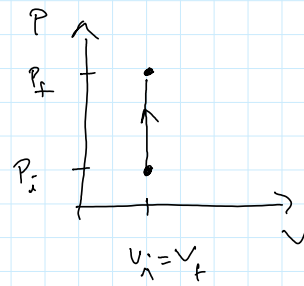
Temp: increases

E_{int} : increases

Pressure: increases

Volume: same

Sketch on a PV diagram:



Work done on the gas in Process 2: $W = 0$

Q is heat transferred to the gas $\left\{ \begin{array}{l} \text{into gas is } + \\ \text{out to environment } - \end{array} \right.$

1st Law of Thermodynamics: Conservation of energy

$$\Delta E_{\text{int}} = Q + W_{\text{on system}}$$

OR

$$\Delta E_{\text{int}} = Q - W_{\text{by system}}$$